

Valda uppgifter i kursboken Matematik M3c av Sjunnesson med flera utgiven på Liber, (2012).

Test 2 ..... 1

2127. a)

$$\begin{aligned}(\sqrt{a} + \sqrt{b})^2 - (\sqrt{a} - \sqrt{b})^2 &= a + 2\sqrt{ab} + b - (a - 2\sqrt{ab} + b) = \\ &= a + 2\sqrt{ab} + b - a + 2\sqrt{ab} - b = 4\sqrt{ab}\end{aligned}$$

b)

$$(1 + \sqrt{3})^4 - 16\sqrt{3} = 1 + 4\sqrt{3} + 6 \cdot 3 + 4 \cdot 3\sqrt{3} + 9 - 16\sqrt{3} = 28$$

2128. Använd Pythagoras sats tre gånger och kombinera ihop.

$$\begin{aligned}d_1^2 &= (a + x)^2 + h^2 \text{ och } d_2^2 = (a - x)^2 + h^2 \Rightarrow \\ d_1^2 + d_2^2 &= a^2 + 2ax + x^2 + a^2 + 2ax + x^2 + 2h^2 = 2a^2 + 2x^2 + 2h^2 \\ \text{men } b^2 &= h^2 + x^2 \text{ dvs } d_1^2 + d_2^2 = 2a^2 + 2b^2 \text{ VSV}\end{aligned}$$

2129.

$$\begin{aligned}h^4 + 9 = 10h^2 &\Leftrightarrow h^4 - 10h^2 + 9 = 0 \Rightarrow h^2 = 5 \pm \sqrt{5^2 - 9} = 5 \pm 4 \Rightarrow \\ &\Rightarrow \begin{cases} h_1^2 = 9 \\ h_2^2 = 1 \end{cases} = \begin{cases} h_1 = \pm 3 \\ h_2 = \pm 1 \end{cases}\end{aligned}$$

2138. a)

$$1 - y^4 = (1 + y^2)(1 - y^2) = (1 + y^2)(1 + y)(1 - y)$$

b)

$$48t^5 - 3t = 3t(16t^4 - 1) = 3t(4t^2 + 1)(4t^2 - 1) = 3t(4t^2 + 1)(2t + 1)(2t - 1)$$

c)

$$\begin{aligned}x^{80} - 1 &= (x^{40} + 1)(x^{40} - 1) = (x^{40} + 1)(x^{20} + 1)(x^{20} - 1) = \\ &= (x^{40} + 1)(x^{20} + 1)(x^{10} + 1)(x^{10} - 1) = \\ &= (x^{40} + 1)(x^{20} + 1)(x^{10} + 1)(x^5 + 1)(x^5 - 1)\end{aligned}$$

2215.

$$f(x) = 3x + 16 \text{ och } g(x) = 2x - 3 \Rightarrow g(f(x)) = g(x) \text{ blir}$$

$$2(3x + 16) - 3 = 2x - 3 \Leftrightarrow 3x + 16 = x \Rightarrow x = -8$$

2216. Det är fel i uppgiften, det borde stått:  $ax^n + bx^{n-1} + cx^{n-2}$

$$x^{3-n}(ax^n + bx^{n-1} + cx^{n-2}) = ax^3 + bx^2 + cx$$

2232.

$$(x - 4)x\left(x + \frac{1}{2}\right) = 0$$

2233.

$$2x^2 - 12x - 14 = 2(x^2 - 6x - 7) = 0$$

Nollställen hittas som:

$$x = 3 \pm \sqrt{9 + 7} = 3 \pm 4 \Rightarrow$$

$$2x^2 - 12x - 14 = 2(x + 1)(x - 7)$$

2234.

$$x(x - 3)^2 = 0$$

2235. a)

$$x^3 - 6x^2 + 10x = x(x^2 - 6x + 10)$$

b)

$$2x^2 - 16x + 14 = 2(x^2 - 8x + 7)$$

Nollställen hittas som:

$$x = 4 \pm \sqrt{16 - 7} = 4 \pm 3 \Rightarrow$$

$$= 2(x - 7)(x - 1)$$

c)

$$x^2 + 36x - 12x = x^2 + 24x = x(x + 24)$$

d)

$$24 - 5x - x^2 = -(x^2 + 5x - 24)$$

Nollställen hittas som:

$$x = -2.5 \pm \sqrt{2.5^2 + 24} = -2.5 \pm 5.5 \Rightarrow$$

$$-(x^2 + 5x - 24) = -(x + 8)(x - 3) = (x + 8)(3 - x)$$

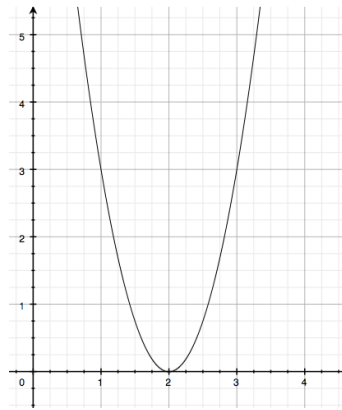
2236. a)

$$4x = x^2 \Rightarrow x = 4 \text{ l. e. (eller } x = 0)$$

b)

$$6x^2 = x^3 \Rightarrow x = 6 \text{ l. e.}$$

2237. Ta till exempel  $f(x) = 3(x - 2)^2$ :



2238.

$$x^2 + bx + c = 0 \text{ dvs } (x - b)(x - c) = 0$$

$$x - x(b + c) + bc = 0 \Rightarrow \begin{cases} b = 1 \\ c = -2 \end{cases}$$

2316.

$$\frac{12}{x - 2}$$

## Test 2

1. a)  $2x - 6 = 2(x - 3)$     b)  $6ab + 8b = 2b(3a + 4)$

c)  $3x^4 - 6x^2 = 3x^2(x^2 - 2) = 3x^2(x - \sqrt{2})(x + \sqrt{2})$

2.a)  $1 - x^2 = (1 + x)(1 - x)$                       b)  $x^2 + 6x + 9 = (x + 3)^2$

c)  $3 - 12x^2 = 3(1 - 4x^2) = 3(1 - 2x)(1 + 2x)$

3. a)

$$\frac{x \cdot x^{-4.2} \cdot x^{0.3}}{x^{-1.9}} = x^{1+0.3+1.9-4.2} = x^{-1}$$

b)

$$\frac{(a^5 b^{-1.5})^4}{a^4 \cdot b^{-6}} = \frac{a^{20} b^{-6}}{a^4 b^{-6}} = a^{16}$$

c)

$$\frac{(6a^2 b^3)^3}{(3a^{-2})^3 (4b^{0.5})^2} = \frac{6 \cdot 6 \cdot 6 \cdot a^6 b^9}{3 \cdot 3 \cdot 3 \cdot a^{-6} 4 \cdot 4 \cdot b} = \frac{a^{12} b^8}{2}$$

4.

$$x^4 + 3x^3 + 2x^2 + x + 1$$

5.

a)  $x_1 = -1$  och  $x_2 = 2$     b)  $0 < x < 2$                       c)  $x < 2$

d)  $x_1 = -1$  och  $x_2 = 3$     e)  $x = 2$

f)  $x < -1$  och  $x > 3$

g)  $f(1) = -1$

6. a)  $|-8| = 8$

b)  $|3 - 5| = |-2| = 2$

7. a)

$$4(3x + 1)(3x - 1) - (4x + 1)(9x - 4) = 4(9x^2 - 1) - (36x^2 - 16x + 9x - 4) =$$

$$= 36x^2 - 4 - 36x^2 + 7x + 4 = 7x$$

b)

$$(3x - 2)^2 + (4x - 1)^2 - (5x - 2)^2 =$$

$$= 9x^2 - 12x + 4 + 16x^2 - 8x + 1 - (25x^2 - 20x + 4) =$$

$$= 25x^2 - 20x + 5 - 25x^2 + 20x - 4 = 1$$

8. a)  $|2| - |7| = 2 - 7 = -5$  och  $|2 - 7| = |-5| = 5$

b)  $|-2| - |5| = 2 - 5 = -3$  och  $|-2 - 5| = |-7| = 7$

9. a)

$$\frac{2 - x}{x^2 - 25} = \frac{2 - x}{(x + 5)(x - 5)} \text{ odefinierad f\u00f6r } x_1 = -5, x_2 = 5$$

b) Definierad f\u00f6r alla reella  $x$ .

10. a)  $f(-2) = 2(-2)^2 - 3(-2) + 2 = 8 + 6 + 2 = 16$

b)  $f(a) = 2a^2 - 3a + 2$

c)  $f(a^2) = 2(a^2)^2 - 3a^2 + 2 = 2a^4 - 3a^2 + 2$

d)  $f(a + h) - f(a) = 2(a + h)^2 - 3(a + h) + 2 - (2a^2 - 3a + 2) =$

$$= 2(a^2 + 2ah + h^2) - 3(a + h) + 2 - (2a^2 - 3a + 2) =$$

$$= 2a^2 + 4ah + 2h^2 - 3a - 3h + 2 - 2a^2 + 3a - 2 = 4ah + 2h^2 - 3h$$

11. a)  $|x - 5| = 10 = \begin{cases} x_1 - 5 = 10 \\ x_2 - 5 = -10 \end{cases} = \begin{cases} x_1 = 15 \\ x_2 = -5 \end{cases}$

b)  $|7 - x| = 4 = \begin{cases} 7 - x_1 = 4 \\ 7 - x_2 = -4 \end{cases} = \begin{cases} x_1 = 3 \\ x_2 = 11 \end{cases}$

12. a)

$$\frac{\frac{x^2 - x}{x + 1}}{x - 1} = \frac{x^2 - x}{x + 1} \cdot \frac{1}{x - 1} = \frac{x(x - 1)}{x + 1} \cdot \frac{1}{x - 1} = \frac{x}{x + 1}$$

b)



$$\frac{7}{10} + \frac{\frac{1}{2x}}{\frac{5}{3x}} = \frac{7}{10} + \frac{1}{2x} \cdot \frac{3x}{5} = \frac{7}{10} + \frac{13}{25} = 1$$

13. a)

$$\frac{3}{x-1} - \frac{2}{x} = \frac{3x}{x(x-1)} - \frac{2(x-1)}{x(x-1)} = \frac{3x - 2(x-1)}{x(x-1)} = \frac{x+2}{x(x-1)}$$

b)

$$\frac{(x+3)^2}{x^2} - \left(1 + \frac{9}{x^2}\right) = \frac{(x+3)^2}{x^2} - \frac{x^2+9}{x^2} = \frac{x^2+6x+9-x^2-9}{x^2} = \frac{6}{x}$$

14. a)

$$\frac{1}{p^2-1} + \frac{1}{p+1} = \frac{1}{p^2-1} + \frac{p-1}{(p+1)(p-1)} = \frac{p}{p^2-1}$$

b)

$$\frac{1}{x+h} - \frac{1}{x} = \frac{x}{x(x+h)} - \frac{x+h}{x(x+h)} = -\frac{h}{x(x+h)}$$

15. a)

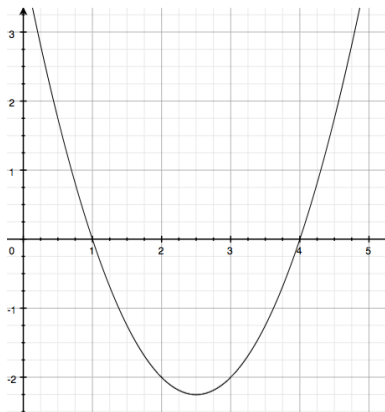
$$x^2 + 8x + 15 = 0 \Rightarrow x = -4 \pm \sqrt{4^2 - 15} = -4 \pm 1 \Rightarrow$$

$$x^2 + 8x + 15 = (x+5)(x+3)$$

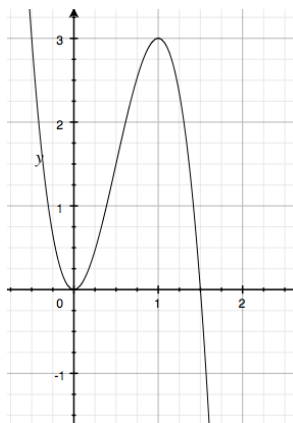
b)

$$2x^3 - 10x^2 + 12x = 2x(x^2 - 5x + 6) = 2x(x-3)(x-2)$$

16. a) Uttrycket byter tecken då  $x = 4$  och då  $x = 1$ . För stora negativa  $x$  är uttrycket  $> 0$ . För stora positiva  $x$  är uttrycket  $> 0$ . Uttrycket är  $< 0$  då  $1 < x < 4$ .

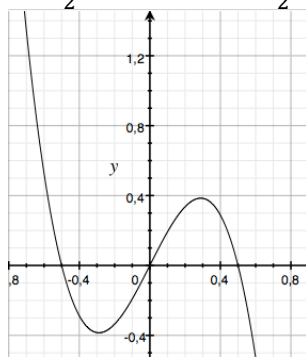


b)  $9x^2 - 6x^3 < 0 \Rightarrow 3x^2(3 - 2x) < 0$  byter tecken då  $x = 1.5$ ,  $3x^2(3 - 2x) < 0$  då  $x > 1.5$ .



17. a)  $x^2 > 6x \Rightarrow x > 6$  eller  $x < 0$

b)  $2x - 8x^3 < 0 \Rightarrow 1 < 4x^2 \Rightarrow x < -\frac{1}{2}$  eller  $0 < x < \frac{1}{2}$



18. a)

$$\frac{6}{2x} + \frac{3}{x} = \frac{3}{2} \Rightarrow 2x \left( \frac{6}{2x} + \frac{3}{x} \right) = 2x \frac{3}{2} \Rightarrow 6 + 6 = 3x \Rightarrow x = 4$$

b)

$$\frac{1}{2y-1} + \frac{1}{1+2y} - \frac{1}{y+2} = 0 \Rightarrow$$

$$\frac{(1+2y)(y+2) + (2y-1)(y+2) - (1+2y)(2y-1)}{(2y-1)(1+2y)(y+2)} = 0$$

$$(1+2y)(y+2) + (2y-1)(y+2) - (1+2y)(2y-1) = 0$$

$$y+2+2y^2+4y+2y^2+4y-y-2-(2y-1+4y^2-2y) = 0$$

$$4y^2+8y-2y+1-4y^2+2y = 0$$

$$8y+1 = 0 \Rightarrow y = -\frac{1}{8} = -0.125$$

19.

$$\frac{1}{b-1} + \frac{2}{b+1} - \frac{3}{b} = \frac{b(b+1) + 2b(b-1) - 3(b-1)(b+1)}{b(b-1)(b+1)} =$$

$$= \frac{b^2+b+2b^2-2b-3(b^2-1)}{b(b^2-1)} = \frac{3-b}{b(b^2-1)}$$

20. a) och b)

$$\frac{\frac{h^2 - h}{h + 1}}{h^3 - h} = \frac{h(h - 1)}{h(h - 1)(h + 1)^2} = \left\{ \begin{array}{l} h \neq 0 \\ h \neq 1 \\ h \neq -1 \end{array} \right\} = \frac{1}{(h + 1)^2} > 0 \text{ om } h \neq -1$$

21.

$$\frac{x^2 + 45x + 200}{x^2 - 25} = x, x^2 + 45x + 200 = 0, x = -22.5 \pm 17.5 = \begin{cases} -5 \\ -40 \end{cases}$$

$$\frac{(x + 5)(x + 40)}{(x + 5)(x - 5)} = x, x \neq -5 \Rightarrow x + 40 = x^2 - 5x$$

$$x^2 - 6x - 40 = 0 \Rightarrow x = 3 \pm 7 = \begin{cases} x_1 = 10 \\ x_2 = -4 \end{cases}$$

## Blandade uppgifter 2

20. a)  $x^2 + 2x > 0 \Leftrightarrow x(x + 2) > 0$  Gör ett teckenschema:

	-3	-2	-1	0	1
$x$	-	-	-	0	+
$x + 2$	-	0	+	+	+
produkt	+	0	-	0	+

$$x^2 + 2x > 0 \text{ då } x < -2 \text{ eller } x > 0$$

b)  $x^2 \leq x \Leftrightarrow x(x - 1) \leq 0$  Gör ett teckenschema:

	-1	0	0.5	1	2
$x$	-	0	+	+	+
$x - 1$	-	-	-	0	+
produkt	+	0	-	0	+

Svar:  $0 \leq x \leq 1$

21. a)  $4x - 6x^2 < 0 \Leftrightarrow 4x(1 - 1.5x) < 0$  Gör ett teckenschema:

	-1	0	1/3	2/3	1
$x$	-	0	+	+	+
$1 - 1.5x$	+	+	+	0	-
produkt	-	0	+	0	-

Svar:  $x < 0$  eller  $x > 2/3$

b)  $x^2 + x < 2 \Leftrightarrow x^2 + x - 2 < 0 \Leftrightarrow (x - 1)(x + 2) < 0$  Gör ett teckenschema:

	-3	-2	0	1	2
$x + 2$	-	0	+	+	+
$x - 1$	-	-	-	0	+
produkt	+	0	-	0	+

Svar:  $-2 < x < 1$

22. a)  $(2 - x)(3 + x) > 0$  Gör ett teckenschema:

	-4	-3	0	2	3
$2 - x$	+	+	+	0	-
$3 + x$	-	0	+	+	+
produkt	-	0	+	0	-

Svar:  $-3 < x < 2$

b)  $4x - x^3 < 0 \Leftrightarrow x(4 - x^2) = x(2 + x)(2 - x) < 0$  Gör ett teckenschema:

	-3	-2	-1	0	1	2	3
$x$	-	-	-	0	+	+	+
$2 - x$	+	+	+	+	+	0	-
$2 + x$	-	0	+	+	+	+	+
produkt	+	0	-	0	+	0	-

Svar:  $-2 < x < -0$  eller  $x > 2$

23.

$$\frac{x}{x^2 - h^2} - \frac{1}{x + h} = \frac{x}{(x + h)(x - h)} - \frac{x - h}{(x + h)(x - h)} = \frac{h}{(x + h)(x - h)}$$

24. Till exempel:

$$\frac{-6}{x - 3} = \frac{6}{3 - x}$$

25. a)

$$\frac{x^2 - 6x + 9}{x} \bigg/ \frac{x^2 - 9}{2x} = \frac{(x - 3)^2}{x} \cdot \frac{2x}{(x - 3)(x + 3)} = \frac{2(x - 3)}{x + 3}$$

b)

$$\frac{x^2 - 2xy}{x + y} \bigg/ \frac{x - 2y}{x^2 - y^2} = \frac{x(x - 2y)}{x + y} \cdot \frac{(x - y)(x + y)}{x - 2y} = x(x - y)$$

26. a)

$$\frac{9 - a^2}{2} / (a^2 - 6a + 9) = \frac{(3 - a)(3 + a)}{2(a - 3)^2} = \frac{3 + a}{2(3 - a)}$$

b)

$$\frac{\frac{a}{3} + \frac{a}{4}}{\frac{a}{3} - \frac{a}{4}} = \frac{\frac{4a}{12} + \frac{3a}{12}}{\frac{4a}{12} - \frac{3a}{12}} = \frac{7a}{a} = 7$$

27. a)  $x^3 - 8x^2 = -7x \Rightarrow x(x^2 - 8x + 7) = 0 \Rightarrow x(x - 1)(x - 7) = 0$

$$x_1 = 0, x_2 = 1 \text{ och } x_3 = 7$$

b)  $4x^3 - 4x^2 + x = 0 \Rightarrow x(4x^2 - 4x + 1) = x(2x - 1)^2 = 0$

$$x_1 = 0, x_2 = x_3 = \frac{1}{2}$$

c)  $4x^2 - 12x^3 = 4x^2(1 - 3x) = 0 \Rightarrow x_1 = x_2 = 0, x_3 = \frac{1}{3}$

28. a)

$$8x - \frac{1}{2x} = 0 \Rightarrow 8x = \frac{1}{2x} \Rightarrow x^2 = \frac{1}{16} \Rightarrow x = \pm \frac{1}{4}$$

b)

$$\frac{y}{y-2} - \frac{3}{y} = 1 \Rightarrow y^2 - 3(y-2) = y^2 - 2y \Rightarrow y = 6$$

c)

$$\frac{1}{1-x} + \frac{1}{1+x} = 3 \Rightarrow 1+x+1-x = 3-3x^2 \Rightarrow x = \pm \frac{1}{\sqrt{3}}$$

29. a)  $|x - 8| = 5 \Rightarrow \begin{cases} x_1 - 8 = -5 \\ x_2 - 8 = 5 \end{cases} \Rightarrow \begin{cases} x_1 = 3 \\ x_2 = 13 \end{cases}$

b)  $|2x - 3| = 2 \Rightarrow \begin{cases} 2x_1 - 3 = -2 \\ 2x_2 - 3 = 2 \end{cases} \Rightarrow \begin{cases} x_1 = 1/2 \\ x_2 = 5/2 \end{cases}$

c)  $|1 - x| = x \Rightarrow \begin{cases} 1 - x_1 = x_1 \\ 1 - x_2 = -x_2 \end{cases} \Rightarrow \begin{cases} x_1 = 1/2 \\ \text{saknar lösning} \end{cases}$

30. a)

$$\frac{4}{x-2} - \frac{8}{x(x-2)} = \frac{4x-8}{x(x-2)} = \frac{4(x-2)}{x(x-2)} = \frac{4}{x}$$

Ej definierat då  $x = 0$ .

b) Se a).

31.

$$\frac{(8-2x)^4}{(4-x)^5} = \frac{2^4(4-x)^4}{(4-x)^5} = \frac{16}{4-x}$$

32.

$$p(p(-1)) = p\left(\frac{1+1}{-1}\right) = p(-2) = \frac{4+1}{-2} = -\frac{5}{2}$$

33.

$$H_B - H_A = \frac{2n(2n-1)}{2} - \frac{n(n-1)}{2} = \frac{4n^2 - 2n - n^2 + n}{2} = \frac{3n^2 - n}{2}$$

34. a)  $12 - 4x - x^2 = \{\text{sök nollställen hos andragradsuttrycket}\} = (2-x)(6+x)$

b)  $2x^3 + 16x - 18x^2 = 2x(x^2 - 9x + 8) = 2x(x-1)(x-8)$

c)  $15x - 2x^2 - x^3 = -x(x^2 + 2x - 15) = -x(x-3)(x+5)$

35. a)

$$\frac{x^3 - 7x^2 - 18x}{2x^2 - 20x + 18} = \frac{x(x^2 - 7x - 18)}{2(x^2 - 10x + 9)} = \frac{x(x+2)(x-9)}{2(x-1)(x-9)} = \frac{x(x+2)}{2(x-1)}$$

b)

$$\frac{x^2 - 10x + 24}{x-4} + 6 = \frac{(x-4)(x-6)}{x-4} + 6 = x - 6 + 6 = x$$

36. a)

$$\frac{x^2 + x - 6}{x-2} + \frac{x^2 + 2x - 15}{x+5} = \frac{(x-2)(x+3)}{x-2} + \frac{(x-3)(x+5)}{x+5} = 2x$$

b)

$$\begin{aligned} \frac{x^2 - x - 12}{x^2 + 10x + 21} + \frac{4x - 4}{x^2 + 6x - 7} - \frac{x}{x+7} &= \frac{(x-4)(x+3)}{(x+3)(x+7)} + \frac{4(x-1)}{(x+7)(x-1)} - \frac{x}{x+7} = \\ &= \frac{x-4}{x+7} + \frac{4}{x+7} - \frac{x}{x+7} = 0 \end{aligned}$$

37.

$$\frac{2}{x+1} + \frac{4}{x+2} = \frac{6}{x+3} \Leftrightarrow$$

$$\Leftrightarrow \frac{2(x+2)(x+3)}{(x+1)(x+2)(x+3)} + \frac{4(x+1)(x+3)}{(x+1)(x+2)(x+3)} = \frac{6(x+1)(x+2)}{(x+1)(x+2)(x+3)} \Leftrightarrow$$

$$\Leftrightarrow 2(x+2)(x+3) + 4(x+1)(x+3) = 6(x+1)(x+2) \Leftrightarrow$$

$$\Leftrightarrow x^2 + 5x + 6 + 2x^2 + 8x + 6 = 3x^2 + 9x + 6 \Leftrightarrow 4x = -6 \Leftrightarrow x = -\frac{3}{2}$$

38.

$$\begin{cases} 2a + 2b = 86 \\ ab = 420 \end{cases} \Rightarrow 2a + 2\frac{420}{a} = 86 \Rightarrow a^2 - 43a + 420 = 0 \Rightarrow$$

$$a = 21.5 \pm \sqrt{21.5^2 - 420} \Rightarrow \begin{matrix} a_1 = 28 \text{ m} \\ a_2 = 15 \text{ m} \end{matrix} \text{ svar: sidorna är 15 och 28 m}$$

39.

$$\begin{aligned} \frac{f(2+h) - f(2)}{h} &= \frac{1}{h} \left( \frac{1}{2+h-1} - \frac{1}{2-1} \right) = \frac{1}{h} \left( \frac{1}{1+h} - 1 \right) = \frac{1}{h} \left( \frac{1}{1+h} - \frac{1+h}{1+h} \right) = \\ &= \frac{1-h}{h(1+h)} = -\frac{1}{1+h} \end{aligned}$$

40.

$$(x + \sqrt{x})^2 - (x - \sqrt{x})^2 = x^2 + 2x\sqrt{x} + x - x^2 + 2x\sqrt{x} - x = 4x\sqrt{x} \text{ VSV}$$

41.

$$\begin{aligned} x^2 + y^2 &= \left( \frac{1-a^2}{1+a^2} \right)^2 + \left( \frac{2a}{1+a^2} \right)^2 = \frac{1-2a^2+a^4}{(1+a^2)^2} + \frac{4a^2}{(1+a^2)^2} = \\ &= \frac{1+2a^2+a^4}{(1+a^2)^2} = \frac{(1+a^2)^2}{(1+a^2)^2} = 1 \text{ VSV} \end{aligned}$$

42.

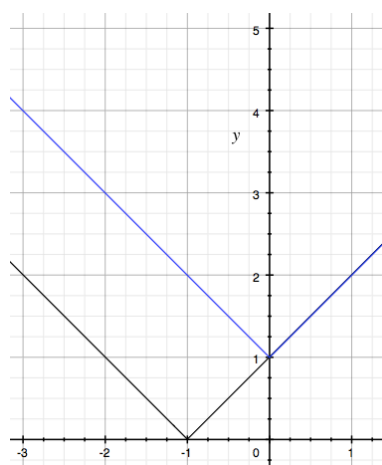
$$p(x) = (2x-1)^2, p(p(-2)) = x^4 \Rightarrow$$

$$p(p(-2)) = (2p(-2)-1)^2 = (2(-2 \cdot 2 - 1)^2 - 1)^2 = x^4 \Rightarrow$$

$$(2(-2 \cdot 2 - 1)^2 - 1)^2 = x^4 \Rightarrow 49^2 = x^4 \Rightarrow x^2 = \pm 49 \Rightarrow x = \begin{cases} \pm 7 \\ \pm 7i \end{cases}$$

43.

$$|x + 1| < |x| + 1$$



I figuren ser man att uttrycket gäller för  $x < 0$ .